

OVERLAPPING GENERATIONS

Methods, Models and
Morphology

Stephen E. Spear and Warren Young

INTERNATIONAL SYMPOSIA IN
ECONOMIC THEORY AND ECONOMETRICS

VOLUME 32

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INTERNATIONAL SYMPOSIA IN ECONOMIC THEORY
AND ECONOMETRICS VOLUME 32

**OVERLAPPING
GENERATIONS:
METHODS, MODELS AND
MORPHOLOGY**

BY

STEPHEN E. SPEAR

Carnegie Mellon University, USA

and

WARREN YOUNG

Bar Ilan University, Israel



United Kingdom – North America – Japan
India – Malaysia – China

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INVESTOR IN PEOPLE

*To our wives, Ann and Sara
Who put up with all the time that went into this work.*

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