

Mean–variance relationship and uncertainty

Mean–variance
relationship

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Abstract

This study investigates the impact of uncertainty on the mean-variance relationship. We find that the stock market's expected excess return is positively related to the market's conditional variances and implied variance during low uncertainty periods but unrelated or negatively related to conditional variances and implied variance during high uncertainty periods. Our empirical evidence is consistent with investors' attitudes toward uncertainty and risk, firms' fundamentals and leverage effects varying with uncertainty. Additionally, we discover that the negative relationship between returns and contemporaneous innovations of conditional variance and the positive relationship between returns and contemporaneous innovations of implied variance are significant during low uncertainty periods. Furthermore, our results are robust to changing the base assets to mimic the uncertainty factor and removing the effect of investor sentiment.

Keywords Economic policy uncertainty, Volatility of volatility, Uncertainty, Mean–variance relationship, Risk–return tradeoff

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1. Introduction

Many studies have shown interest in models with rational investors in financial markets and have developed models to explain anomalies in financial markets. Based on classical finance theories, taking a high risk is compensated with high returns, consistent with a positive mean–variance relationship. However, the ambiguous mean–variance relationship has been argued for decades (French *et al.*, 1987; Campbell, 1987; Turner *et al.*, 1989). Additionally, some literature argues the effect of behavioral biases of investors on the mean–variance relationship (Cohen *et al.*, 2005; Yu and Yuan, 2011; Kim *et al.*, 2017a; Seo *et al.*, 2021) to explain this unclear relationship.

The theory of rational asset pricing insists on a positive mean–variance relationship. Merton (1973) shows a positive relationship between the conditional expected excess stock returns and the conditional variance in the intertemporal capital asset pricing model. The literature, including French *et al.* (1987), Bailie and De Gennaro (1990), Ghysel *et al.* (2005) and Pástor *et al.* (2008), finds empirical evidence supporting this positive mean–variance relationship. However, some studies, including Campbell (1987), Nelson (1991) and Brandt and Kang (2004), discover a negative mean–variance relationship. Turner *et al.* (1989) and Glosten *et al.* (1993) provide empirical evidence of both a positive and negative relationship.

Uncertainty is an important concept in finance, accompanied by much literature on its impact on asset price movements. Buraschi and Jiltsov (2006) show that the model uncertainty induced by heterogeneous agents explains better dynamics of option prices and volume than

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the models with stochastic volatility. Andersen *et al.* (2009) find empirical evidence that uncertainty seems to be different from risk and seems to have a different impact on asset prices, compared with risk. Some literature suggests the measure of uncertainty. Baker *et al.* (2016) develop economic policy uncertainty (EPU) [1] based on news. They show that EPU contains information on the movements in policy-related economic uncertainty. Based on EPU, many studies including Pástor and Veronesi (2013), Brogaard and Detzel (2015) and Aroui *et al.* (2016) confirm that EPU exerts influence on risk premium. In addition, Baltussen *et al.* (2018) propose the measurement of uncertainty about risk, the volatility-of-volatility (VOV) [2], and show that the stocks with low VOV outperform the stocks with high VOV. Based on VOV, Hollstein *et al.* (2019) show that time-varying VOV commands a significant negative risk premium after controlling for volatility and jump risk. Ruan (2020) provides empirical evidence that there is a significant negative relationship between equity option returns and VOV after controlling for numerous option and stock characteristics. In this study, we focus on the influence of uncertainty on the risk–return relationship in the stock market.

Since uncertainty plays an important role in asset pricing, some literature explores the effect of uncertainty on the mean–variance relationship. Yang and Yang (2021) show the impact of EPU on the mean–variance relationship in the Chinese stock market. They find that the stock market’s excess return is positively (negatively) related to conditional variance during low (high) EPU periods. However, they use only one uncertainty measure to provide direct evidence of the mean–variance relationship with conditional variances. Moreover, they do not consider the influence of other factors on the mean–variance relationship, as investigated in previous literature.

This study employs not only EPU but also the VOV to measure uncertainty in the stock market. We utilize the model-free implied variance from the options market as future stock market return variance in addition to four conditional variances estimated based on historical stock market returns. We also check the return–innovation relationship to provide additional indirect empirical evidence of the mean–variance relationship and consider the information of investor sentiment [3] to identify unique information of uncertainty on the mean–variance relationship.

Along with Yang and Yang (2021), we expect high EPU to distort the positive mean–variance relationship. EPU increases investors’ uncertainty aversions and risk perceptions and changes in the firm’s fundamental information [4]. While both EPU and VOV generally contain information on uncertainty, VOV reveals uncertainty about risk, which is different from the government’s policy uncertainty in EPU. Therefore, the mechanism by which VOV affects the stock market’s mean–variance relationship is different from that of the EPU.

In addition, we also conjecture that high VOV weakens the positive mean–variance relationship. Park (2015) shows that the negative skewness in the return distribution is proportional to the VOV, and the excess kurtosis in the return distribution is proportional to the squared VOV. Thus, he proposes VOV as a tail risk indicator in his model and argues that an increase in VOV would raise the prices of tail risk hedging options and lower subsequent returns. The extent of uncertainty about risk is a critical factor for determining the likelihood of meager returns. Through the stochastic channel (i.e. a persistent volatility process with a leverage effect), VOV can reveal the degree of the market’s perception of tail risk incorporated into stock market dynamics. As an increase in VOV associated with the leverage effect of Black (1976) and Christie (1982) causes a negative mean–variance relationship [5], a positive risk–return tradeoff is undermined during the period of high VOV.

Collectively, we hypothesize that a positive relationship between the expected stock market return and variance is invalidated in periods of high uncertainty (i.e. periods of high EPU or high VOV). Still, this relationship is restored in low uncertainty periods (i.e. periods of low EPU or low VOV). Following Yu and Yuan (2011), we analyze the mean–variance relationship within high and low uncertainty regimes to test the hypotheses. In high

uncertainty periods, we find the mean–variance tradeoff to be significantly negative. In contrast, during low uncertainty periods, a positive risk–return tradeoff is observed. Further evidence that the effect of uncertainty is critical for the risk–return tradeoff occurs in the reactions of stock market returns to variance innovations. During periods of high uncertainty, a negative relationship between returns and contemporaneous innovations of conditional variances and a positive relationship between returns and contemporaneous innovations of implied variance are significantly weakened. These results are consistent with changes in investors’ uncertainty aversion, investors’ risk perceptions, the firm’s cash flow risk, investment risk and the leverage effect generated by the uncertainty shock. In low uncertainty periods, the return is negatively related to contemporaneous innovations of conditional variances and positively related to contemporaneous innovations of implied variance, consistent with the positive mean–variance relationship we show during such periods. The results are robust to changing the base assets to construct a mimicking factor for uncertainty and removing the effect of investor sentiment on the mimicking factor for uncertainty.

This study contributes to the literature on uncertainty by proving that uncertainty plays an important role in empirical asset pricing. First, we extend the uncertainty measures beyond EPU. EPU is a news-based measure constructed based on text mining techniques; it lacks investors’ perspectives in the stock market. However, VOV offers various advantages over uncertainty measure based on articles in newspapers: it is *ex ante*, easy to compute, extracted directly from the options market, includes information on future underlying asset movements, available at a daily frequency and circumvents the self-selection problem in articles in newspapers (Just and Crigler, 1989). Additionally, our study suggests a novel mechanism for uncertainty derived from the options market to movements in the stock market. Second, we employ the model-free implied variance extracted from options prices in addition to the conditional variances estimated based on historical stock market returns. Many studies document that implied volatility contains superior information that can help forecast future volatility (Christensen and Prabhala, 1998; Blair *et al.*, 2001; Jiang and Tian, 2005; Busch *et al.*, 2011). Therefore, exploiting the implied variance can help confirm the information of uncertainty on the stock market movements more strongly. Third, we provide additional indirect evidence based on the return–innovation relationship analysis to confirm the impact of uncertainty on a positive risk–return tradeoff. Lastly, as Yu and Yuan (2011) show high sentiment undermines a positive mean–variance tradeoff; we check whether uncertainty has unique and additional information on the risk–return tradeoff beyond investor sentiment.

The remainder of this paper is organized as follows. Section 2 introduces the uncertainty measures and the methodology used to create the mimicking factor for the uncertainty measures. Section 3 describes the data and presents the main empirical results. Section 4 discusses the robustness checks. Finally, Section 5 concludes the paper.

2. Uncertainty and variance

This section introduces the uncertainty measures and the methodology used to form a mimicking factor to track uncertainty. We also introduce the conditional variances and implied variance mainly investigated in this study.

2.1 Uncertainty

2.1.1 *Economic policy uncertainty.* Baker *et al.* (2016) develop an EPU to gauge policy uncertainty shocks. They construct the United States (US) EPU based on search results from articles of 10 prominent newspapers: USA Today, Miami Herald, Chicago Tribune, The

Washington Post, Los Angeles Times, The Boston Globe, San Francisco Chronicle, The Dallas Morning News, Houston Chronicle and The Wall Street Journal. Notably, the US EPU is calculated based on normalizing the number of articles containing at least one term related to economic and policy uncertainty such as “uncertainty” or “uncertain,” “economic” or “economy,” and one or more among the following terms: “congress,” “legislation,” “white house,” “regulation,” “federal reserve” or “deficit.”

2.1.2 Volatility-of-Volatility. Baltussen *et al.* (2018) propose VOV to measure uncertainty about risk. They argue that as VOV gauges dispersed investors’ subjective beliefs about the volatility of expected stock return distribution, it could capture the uncertainty about the risk perceived by investors. Specifically, the implied volatility extracted from options prices is regarded as the expected stock return volatility, and VOV is computed as the standard deviation of implied volatility scaled by average implied volatility. Therefore, we employ the VOV on day t , calculated as follows:

$$VOV_t = \frac{\sqrt{\frac{1}{19} \sum_{i=t-19}^t (\sigma_i - \bar{\sigma}_t^{IV})^2}}{\bar{\sigma}_t^{IV}}, \quad (1)$$

where $\bar{\sigma}_t^{IV} = \frac{1}{20} \sum_{i=t-19}^t \sigma_i$, and σ_i is the implied volatility on day i .

2.1.3 Mimicking factor for uncertainty. Following empirical asset pricing literature, including Ang *et al.* (2006) and Kapadia (2011), we construct a mimicking factor to measure the exposure to uncertainty by estimating the coefficient b' in the following regression:

$$EPU_t(\text{or } VOV_t) = c + b'X_t + u_t, \quad (2)$$

where EPU_t (VOV_t) is the EPU (VOV) in month t , and X_t is the set of returns on the base assets in month t . Following Kapadia (2011), we use the Fama–French three factors as base assets. Based on the estimation of equation (2), the mimicking factor for EPU (FEPU) or VOV (FVOV) in month t is defined as:

$$FEPU_t(\text{or } FVOV_t) = \hat{b}'X_t, \quad (3)$$

where \hat{b}' is the coefficient estimate of b' . Based on FEPU and FVOV, we analyze the effect of uncertainty on the mean–variance relationship.

2.2 Conditional variances and implied variance

2.2.1 Rolling window model. French *et al.* (1987) find empirical evidence of a positive relationship between the expected market risk premium and the volatility estimated by the rolling window model. Following them, we employ the realized variance based on the daily returns in month t as the conditional variance of the return on the next month $t+1$:

$$Var_t(R_{t+1}) = \frac{22}{N_t} \sum_{d=0}^{N_t-1} r_{e(t)-d}^2, \quad (4)$$

where $Var_t(R_{t+1})$ is the estimate of the stock market return variance for the next month $t+1$ based on conditional information at month t . $e(t)$ is the last day of the month t , $r_{e(t)-d}$ is the demeaned return on the day $(e(t)-d)$, with subtraction of the average daily return during month t and N_t is the number of trading days in month t .

2.2.2 *Mixed data sampling model.* Ghysel *et al.* (2005) introduce the mixed data sampling (MIDAS) model to estimate monthly conditional variance forecasts with past daily returns. Following them, we employ the conditional variance estimator of the MIDAS with the exponential Almon lag specifications (Almon, 1965; Judge *et al.*, 1985) as follows:

$$\text{Var}_t(R_{t+1}) = \alpha + \beta \sum_{d=1}^{252} w_d(\kappa_1, \kappa_2) r_{e(t)+1-d}^2, \quad (5)$$

where $w_d(\kappa_1, \kappa_2) = \frac{\exp(\kappa_1 d + \kappa_2 d^2)}{\sum_{i=1}^{252} \exp(\kappa_1 i + \kappa_2 i^2)}$, $e(t)$ is the last day of the month t , and $r_{e(t)+1-d}$ is the return on the day $(e(t)+1-d)$. We obtain the monthly conditional variance forecast using the daily data of the previous 252 days with the parameter estimates from the rolling window estimation with the previous 252 daily observations.

2.2.3 *GARCH model.* Bollerslev (1986) and Taylor (1986) propose the GARCH model to estimate conditional variances by considering the effects of historical variance and return innovation on future variance. In this study, we utilize GARCH(1,1) to estimate daily conditional variances:

$$r_{i+1} = \mu + \varepsilon_{i+1}, \quad \text{where } \varepsilon_{i+1}|I_{i+1} \sim N(0, \sigma_{i+1}^2), \quad (6)$$

$$\sigma_{i+1}^2 = \alpha_G + \beta_G \varepsilon_i^2 + \gamma_G \sigma_i^2, \quad (7)$$

where r_{i+1} is the stock market return on day $i+1$, μ is the conditional mean of the daily stock market returns, σ_{i+1}^2 is the conditional variance of the daily stock market returns on day $i+1$. Thus, I_{i+1} is the information set at day $i+1$, $N(a, b)$ is the normal distribution with mean a and variance b , and ε_{i+1} is the daily stock market return innovation on day $i+1$. We compute the monthly conditional variance forecast based on the daily conditional variance estimates with the parameter estimates from the rolling window estimation with the previous 252 daily observations:

$$\text{Var}_t(R_{t+1}) = E_t \left(\sum_{d=1}^{22} \sigma_{e(t)+d}^2 \right), \quad (8)$$

where $\text{Var}_t(R_{t+1})$ is the estimate of the stock market return variance for the next month $t+1$ based on conditional information at month t , and $e(t)$ is the last day of month t .

2.2.4 *GJR-GARCH model.* Glosten *et al.* (1993) propose the GJR-GARCH model, which allows for different shocks of positive and negative return innovations on return volatility, while the GARCH model does not allow for different shocks. Following Glosten *et al.* (1993), we employ the GJR-GARCH(1,1) to estimate the daily conditional variance as follows:

$$r_{i+1} = \mu + \varepsilon_{i+1}, \quad \text{where } \varepsilon_{i+1}|I_{i+1} \sim N(0, \sigma_{i+1}^2), \quad (9)$$

$$\sigma_{i+1}^2 = \alpha_{GJR} + \beta_{GJR} \varepsilon_i^2 + \gamma_{GJR} D_i \varepsilon_i^2 + \theta_{GJR} \sigma_i^2, \quad (10)$$

where D_i is a dummy variable, the value of which is one when ε_i is negative and the other notations are the same as those in GARCH(1,1). Like the monthly conditional variance forecasts from GARCH(1,1), we calculate the monthly conditional variance estimates based on the daily conditional variance estimates with the parameter estimates of the GJR-GARCH(1,1) from the rolling window estimation with previous 252 daily observations.

2.2.5 *Implied variance.* Jiang and Tian (2005) suggest that model-free implied volatility, independent of option pricing models, has superior forecasting ability for future volatility and

contains more information than the historical volatility and Black–Scholes implied volatility. This study uses the square of the model-free implied volatility as the implied variance.

3. Data and empirical analysis

In this section, we analyze the effect of uncertainty on the risk–return relationship. First, we describe the data for FEPU and FVOV, conditional variances, and implied variance in the US. Second, we test whether uncertainty affects the relationship between expected stock market returns and the variances described in Section 2. Additionally, we check the effect of uncertainty on the relationship between realized excess stock market returns and contemporaneous unexpected volatility innovations to analyze the mean–variance relationship indirectly.

3.1 Data description

Our sample spans from January 2003 to November 2018, with 191 monthly observations. We use monthly returns of the S&P500 index as a proxy for stock market returns and the 3-month treasury bill rate yield as the risk-free rate of stock market returns. These data are obtained from the Chicago Board Options Exchange (CBOE) and the Federal Reserve Bank of St. Louis. The US EPU is obtained from the EPU website [6], and the US VOV is constructed based on the VIX provided by the CBOE. Fama–French three factors are obtained from French’s website to construct the mimicking factor for uncertainty [7]. The conditional variances and implied variance are estimated based on the daily returns of the S&P500 index and VIX, respectively.

Table 1 reports the basic summary statistics for uncertainty and Fama–French three factors. In Panel A, the average and standard deviation of EPU are 121.2328 and 45.7760, respectively. The average and standard deviation of FEPU are -1.2049 and 7.0066, respectively. The difference between EPU and FEPU is similar to those of China in Yang and Yang (2021). The mean and standard deviation of FVOV are smaller than those of VOV. The correlations among uncertainty measures and Fama–French three factors are represented in Panel B. The correlation between EPU and VOV is 0.2444 and significant at the 1% level, indicating that the raw uncertainty measures derived from various sources such as newspapers and options markets capture common uncertainty components. Additionally, as the correlation between FEPU and FVOV is 0.9151 and significant at the 1% level, the mimicking factors for raw uncertainty measures are more positively correlated than the raw uncertainty measures themselves.

Table 2 presents the moments of the monthly excess stock market returns, conditional variances and implied variance. We divide the entire sample period into high and low uncertainty periods depending on the signs of FEPU and FVOV, respectively. If FEPU or FVOV in a month is positive, the month is in a high uncertainty period, and 0 otherwise. Out of the 191 months of the whole sample period, 79 months fall into high uncertainty periods, while 112 months fall into low uncertainty periods based on FEPU. As for FVOV, 68 months fall into high uncertainty periods, while 123 months fall into low uncertainty periods. In periods of high uncertainty, the average monthly excess market returns are lower than those in low uncertainty periods. In contrast, the monthly excess market returns during high uncertainty periods are more volatile than those during low uncertainty periods. However, the mean and standard deviation of conditional variances and implied variance during high uncertainty periods are higher than their counterparts during low uncertainty periods. In summary, during high uncertainty periods, the realized excess stock market returns are lower and more volatile, and the variance estimates are larger.

Table 3 shows the correlations between the monthly excess stock market returns, conditional variances, and implied variance. The correlations between excess stock market returns and conditional variances are negatively significant at the 1% or 5% levels. Though

Panel A: Descriptive statistics							
	Mean	Median	Max	Min	Std. Dev	Skewness	Kurtosis
EPU_t	121.2328	110.7019	283.6656	44.7828	45.7760	0.8535	3.4578
$FEPU_t$	-1.2049	-1.5139	29.4078	-17.9971	7.0066	0.7559	5.3361
VOV_t	0.0930	0.0819	0.4545	0.0296	0.0506	2.6505	16.5365
$FVOV_t$	-0.0033	-0.0043	0.0700	-0.0461	0.0160	0.7005	5.2154
MKT_t	0.0079	0.0118	0.1135	-0.1723	0.03931	-0.7326	5.2188
SMB_t	0.0018	0.0023	0.0613	-0.0478	0.0231	0.1763	2.6288
HML_t	-0.0001	-0.0011	0.0822	-0.1112	0.0241	-0.1202	5.7476

Panel B: Correlations						
	EPU_t	$FEPU_t$	VOV_t	$FVOV_t$	MKT_t	SMB_t
$FEPU_t$	0.1531**					
VOV_t	0.2444***	0.2889***				
$FVOV_t$	0.1401*	0.9151***	0.3157***			
MKT_t	-0.1412*	-0.9223***	-0.3098***	-0.9815***		
SMB_t	-0.0038	-0.0245	-0.0764	-0.2421***	0.3610***	
HML_t	-0.0639	-0.4175***	-0.0305	-0.0966	0.2472***	0.1015

Note(s): The table reports summary statistics of monthly uncertainty variables and the Fama–French three factors in US stock market. Panel A presents descriptive statistics for monthly uncertainty variables and the Fama–French three factors. Panel B presents correlations between monthly uncertainty variables and the Fama–French three factors. EPU_t is the EPU in month t . $FEPU_t$ is the mimicking factor for the EPU in month t . VOV_t is the VOV in month t . $FVOV_t$ is the mimicking factor for the VOV in month t . MKT_t is the market return in excess of risk-free rate in month t . SMB_t is the average return on the three small portfolios minus the average return on the three big portfolios in month t . HML_t is the average return on the two high B/M portfolios minus the average return on the two low B/M portfolios in month t . *, **, and *** represent significance at the 10, 5 and 1% levels, respectively. The sample period covers January 2003 to November 2018

Table 1.
Summary statistics of
uncertainty and Fama–
French three factors

insignificant, the correlation between excess stock market returns and implied variance is negative. The correlations among conditional variances and implied variance range from 0.6935 to 0.9629 and are positively significant at the 1% level. Thus, the correlations in Table 3 indicate a negative mean–variance relationship over the entire sample period, which is inconsistent with the fundamental risk–return tradeoff in finance.

Figure 1 displays the time-series of monthly excess stock market returns, conditional variances and implied variance during high and low uncertainty periods, depending on the sign of FEPU. During low uncertainty periods, the conditional variances and implied variance tend to co-move with stock market returns. However, they move in the opposite direction of stock market returns during periods of high uncertainty. The correlations between stock market returns and variances are positive and statistically significant at the 1% level during periods of low uncertainty. However, the correlations are negative and significant at the 1% or 5% levels in high uncertainty periods, except for the implied variance [8].

Figure 2 illustrates the time-series of monthly excess stock market returns, conditional variances and implied variance during high and low uncertainty periods, depending on the sign of FVOV. As shown in Figure 1, stock market returns tend to move closer to the conditional variances and implied variance during low uncertainty periods than during high uncertainty periods. While the correlations between stock market returns and variances during low uncertainty periods are positive and significant at the 5% or 10% levels, except for the case of the rolling window model, the correlations between them during high uncertainty periods are negative and significant at the 1% level except for the case of the implied variance [9]. For both FEPU and FVOV, the difference between the patterns of the correlations during high and low uncertainty periods suggests a positive mean–variance

Variable	Mean(%)	Median(%)	Max(%)	Min(%)	Std. Dev.(%)	Skewness	Kurtosis
Panel A: Whole sample period (191 monthly observations)							
R_{t+1}	0.5364	0.8728	10.7706	-16.9984	3.8743	-0.7829	5.2820
$\sigma_{RW, t+1}^2$	0.2801	0.1231	5.4539	0.0138	0.5796	6.0531	46.6412
$\sigma_{M, t+1}^2$	0.3457	0.1430	8.7049	0.0391	0.7787	7.8393	76.4870
σ_G^2	0.2981	0.1419	5.2800	0.0397	0.5856	6.0737	45.1464
$\sigma_{GJR, t+1}^2$	0.2792	0.1654	3.3902	0.0422	0.4441	5.4099	35.8330
$\sigma_{IV, t+1}^2$	4.1351	2.6569	35.8681	0.9044	4.6218	3.8514	21.5677
Panel B: High uncertainty periods with positive $FEPU_t$ (79 monthly observations)							
R_{t+1}	0.3097	0.8423	10.7706	-16.9984	4.9157	-0.6526	4.0718
$\sigma_{RW, t+1}^2$	0.4727	0.2281	5.4539	0.0446	0.8283	4.2532	22.8819
$\sigma_{M, t+1}^2$	0.5140	0.2069	8.7049	0.0573	1.1509	5.4612	35.9613
σ_G^2	0.4566	0.1986	5.2800	0.0584	0.8441	4.2677	21.9725
$\sigma_{GJR, t+1}^2$	0.4285	0.2456	3.3902	0.0623	0.6349	3.7371	17.0246
$\sigma_{IV, t+1}^2$	5.9205	3.9402	35.8681	1.1707	6.1749	2.8557	12.1809
Panel C: Low uncertainty periods with negative $FEPU_t$ (112 monthly observations)							
R_{t+1}	0.6963	1.0166	9.3792	-9.3764	2.9412	-0.6396	4.4701
$\sigma_{RW, t+1}^2$	0.1442	0.0914	1.9980	0.0138	0.2188	6.0243	48.2440
$\sigma_{M, t+1}^2$	0.2270	0.1275	1.5481	0.0391	0.2699	3.1271	12.9936
σ_G^2	0.1863	0.1191	2.0411	0.0397	0.2363	5.2797	37.3554
$\sigma_{GJR, t+1}^2$	0.1739	0.1322	1.4297	0.0422	0.1653	4.8534	33.3487
$\sigma_{IV, t+1}^2$	2.8758	2.0867	19.4834	0.9044	2.4292	3.9540	23.8663
Panel D: High uncertainty periods with positive $FVOV_t$ (68 monthly observations)							
R_{t+1}	0.3887	0.7338	10.7706	-16.9984	4.6578	-0.7512	5.0119
$\sigma_{RW, t+1}^2$	0.4810	0.2253	5.4539	0.0267	0.8679	4.2022	21.8380
$\sigma_{M, t+1}^2$	0.5232	0.1813	8.7049	0.0869	1.2324	5.1580	31.7502
σ_G^2	0.4675	0.1689	5.2800	0.0826	0.9037	4.0162	19.3136
$\sigma_{GJR, t+1}^2$	0.4405	0.2190	3.3902	0.0831	0.6782	3.5215	14.9894
$\sigma_{IV, t+1}^2$	6.0566	3.8133	35.8681	1.4496	6.4383	2.8337	11.6743
Panel E: Low uncertainty periods with negative $FVOV_t$ (123 monthly observations)							
R_{t+1}	0.6181	1.0554	9.3792	-9.3764	3.3827	-0.6968	4.2307
$\sigma_{RW, t+1}^2$	0.1690	0.0934	2.0075	0.0138	0.2732	5.2131	34.0925
$\sigma_{M, t+1}^2$	0.2476	0.1393	1.5481	0.0391	0.2882	2.7451	10.3425
σ_G^2	0.2045	0.1254	2.0411	0.0397	0.2465	4.4355	28.5622
$\sigma_{GJR, t+1}^2$	0.1901	0.1356	1.4297	0.0422	0.1789	3.8126	22.4139
$\sigma_{IV, t+1}^2$	3.0729	2.1433	19.4834	0.9044	2.7033	3.4404	17.9136

Note(s): The table reports descriptive statistics of monthly excess stock market returns, conditional variances, and implied variance. R_{t+1} is the monthly excess stock market returns in month $t+1$. $\sigma_{RW, t+1}^2$ is the conditional variance in month $t+1$ estimated by the rolling window model. $\sigma_{M, t+1}^2$ is the conditional variance in month $t+1$ estimated by the MIDAS. σ_G^2 is the conditional variance in month $t+1$ estimated by the GARCH(1,1). $\sigma_{GJR, t+1}^2$ is the conditional variance in month $t+1$ estimated by the GJR-GARCH(1,1). $\sigma_{IV, t+1}^2$ is the implied variance in month $t+1$ calculated by the square of VIX_t . Panel A reports the descriptive statistics during the whole sample period. Panel B and Panel D report the descriptive statistics during high uncertainty periods with positive $FEPU_t$ and positive $FVOV_t$, respectively. Panel C and Panel E report the descriptive statistics during low uncertainty periods with negative $FEPU_t$ and negative $FVOV_t$, respectively. The sample period is from January 2003 to November 2018

Table 2.
Descriptive statistics of monthly excess stock market returns, conditional variances and implied variance

relationship in low uncertainty periods. Still, this relationship deteriorates in periods of high uncertainty.

3.2 Mean–variance relation

The mean–variance relationship has been analyzed with the following regression:

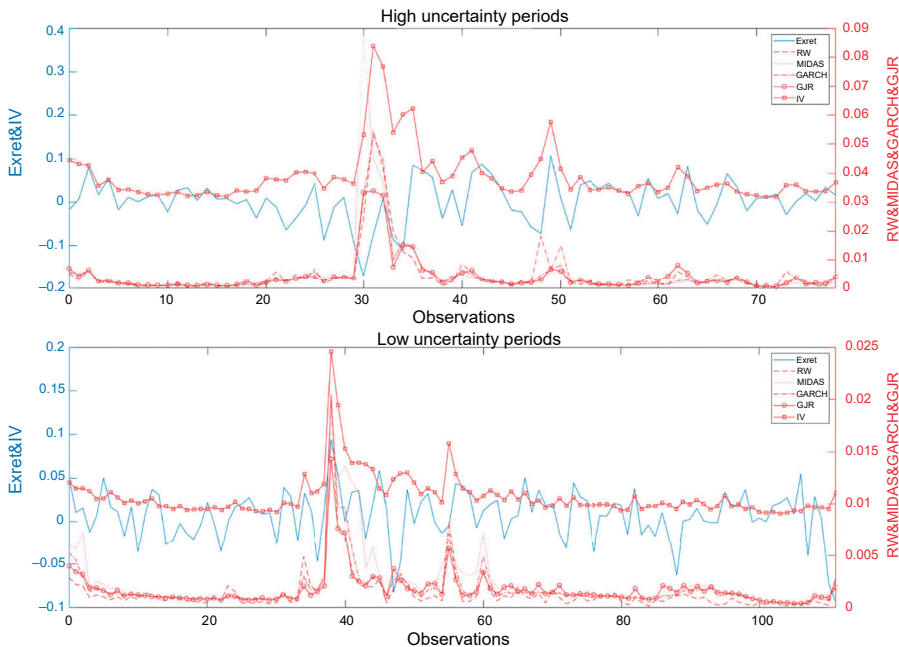
$$R_{t+1} = a + bVar_t(R_{t+1}) + \varepsilon_{t+1}, \quad (11)$$

where R_{t+1} is the monthly excess stock market return, and $Var_t(R_{t+1})$ is the conditional variance or implied variance of the stock market returns for the next month $t+1$ based on

	R_{t+1}	$\sigma_{RW, t+1}^2$	$\sigma_{M, t+1}^2$	σ_G^2	$\sigma_{GJR, t+1}^2$
$\sigma_{RW, t+1}^2$	-0.2122***				
$\sigma_{M, t+1}^2$	-0.2795***	0.7587***			
σ_G^2	-0.1738**	0.9564***	0.8389***		
$\sigma_{GJR, t+1}^2$	-0.1917***	0.9117***	0.9019***	0.9629***	
$\sigma_{IV, t+1}^2$	-0.0545	0.8976***	0.6935***	0.8927***	0.8888***

Note(s): The table reports correlations between monthly excess stock market returns, conditional variances and implied variance. All variable definitions are identical to those in Table 2. ** and *** represent significance at the 5 and 1% levels, respectively

Table 3. Correlations of monthly excess stock market returns, conditional variances and implied variance



Note(s): This figure plots the time-series of monthly excess stock market returns, conditional variances, and implied variance during high (i.e. $FEPU_t > 0$) and low (i.e., $FEPU_t \leq 0$) uncertainty periods. The left scale presents excess stock market returns and implied variance, and the right scale presents conditional variances. The sample period covers January 2003 to November 2018, with 191 monthly observations

Figure 1. Time-series of monthly excess stock market returns, conditional variances and implied variance with FEPU

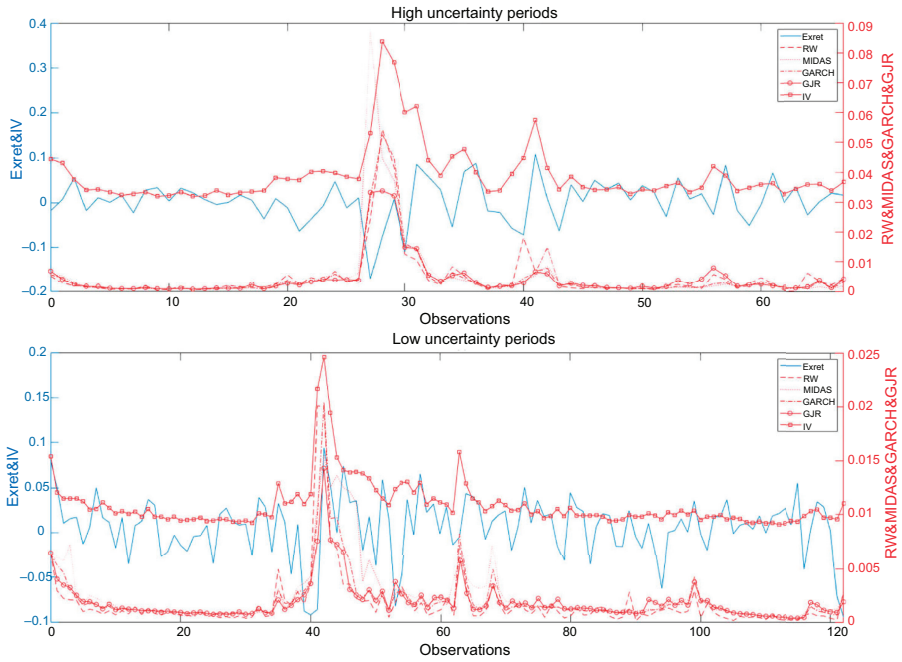


Figure 2. Time-series of monthly excess stock market returns, conditional variances and implied variance with FVOV

Note(s): This figure plots the time-series of monthly excess stock market returns, conditional variances, and implied variance during high (i.e., $FVOV_t > 0$) and low (i.e., $FVOV_t \leq 0$) uncertainty periods. The left scale presents excess stock market returns and implied variance, and the right scale presents conditional variances. The sample period covers January 2003 to November 2018, with 191 monthly observations

conditional information at month t . To analyze the effect of uncertainty on this mean–variance relationship, we conduct the following two-regime equation:

$$R_{t+1} = a_1 + b_1 Var_t(R_{t+1}) + a_2 D_t + b_2 D_t Var_t(R_{t+1}) + \varepsilon_{t+1}, \quad (12)$$

where D_t is a dummy variable for the high uncertainty regime, the value of which equals 1 if month t is included in high uncertainty periods, and 0 otherwise [10, 11]

Table 4 reports the coefficient estimates and t -statistics for the one-regime and two-regime equations. In the one-regime equation, the coefficient estimates (b) on the conditional variances estimated by the rolling window model and MIDAS are negative and significant at the 1% or 5% levels, as expected. Although insignificant, the coefficient estimates (b) on the conditional variances of GARCH(1,1) and GJR-GARCH(1,1) and implied variance are negative. The adjusted R^2 s of the one-regime equation range from -0.230% to 7.322% . Therefore, we confirm that a positive mean-variance tradeoff is reversed.

The results from the two-regime equation support our expectation that the mean-variance tradeoff varies with the degree of uncertainty. In low uncertainty periods, we find a significant positive tradeoff in models (1)-E, (2)-E, (2)-V, (3)-E, (3)-V, (4)-E, and 5-(E). Although the mean–variance relation is insignificant during low uncertainty periods in models (1)-V, (4)-V, and (5)-V, the coefficient estimates (b_1) are positive. In periods of high uncertainty, such a positive tradeoff is strongly undermined because the coefficient estimates (b_2) on the

Model	$a(a_1)$	$b(b_1)$	a_2	b_2	Adj. R^2 (%)
<i>Panel A: Rolling window model</i>					
(1)	0.0093 ^{***} (4.2790)	-1.4184 ^{***} (-2.6544)			3.998
(1)-E	0.0016 (0.6460)	3.7435 ^{***} (3.9470)	0.0108 [*] (1.6542)	-5.6970 ^{***} (-6.8944)	8.572
(1)-V	0.0049 ^{**} (2.2718)	0.7455 (0.5562)	0.0079 [*] (1.8228)	-2.6120 ^{**} (-2.0728)	4.922
<i>Panel B: MIDAS</i>					
(2)	0.0102 ^{***} (4.7540)	-1.3904 ^{**} (-2.0073)			7.322
(2)-E	2.00×10^{-5} (0.0074)	3.0585 ^{***} (5.5544)	0.0120 ^{**} (2.0444)	-4.7987 ^{***} (-8.4804)	12.482
(2)-V	7.25×10^{-4} (0.2404)	2.2035 [*] (1.6617)	0.0124 ^{**} (2.5079)	-3.9700 ^{***} (-3.3228)	11.542
<i>Panel C: GARCH(1,1)</i>					
(3)	0.0088 ^{***} (4.4181)	-1.1497 (-1.3162)			2.507
(3)-E	2.55×10^{-4} (0.0945)	3.5999 ^{***} (5.0673)	0.0104 [*] (1.8016)	-5.2620 ^{***} (-7.6733)	6.973
(3)-V	6.86×10^{-4} (0.2572)	2.6870 [*] (1.8149)	0.0111 ^{**} (2.3772)	-4.3717 ^{***} (-3.5855)	5.917
<i>Panel D: GJR-GARCH(1,1)</i>					
(4)	0.0100 ^{***} (4.3402)	-1.6726 (-1.1836)			3.166
(4)-E	-0.0013 (-0.3852)	4.7389 ^{***} (3.1716)	0.0143 ^{**} (2.5191)	-7.0444 ^{***} (-4.8563)	7.021
(4)-V	-6.14×10^{-4} (-0.1748)	3.5749 (1.5031)	0.0151 ^{***} (2.7747)	-5.9796 ^{***} (-3.2495)	6.604
<i>Panel E: Implied variance</i>					
(5)	0.0073 ^{***} (2.7026)	-0.0457 (-0.3959)			-0.230
(5)-E	-0.0037 (-1.1008)	0.3719 ^{***} (4.2482)	0.0143 ^{**} (2.1373)	-0.4979 ^{***} (-3.1338)	3.553
(5)-V	-8.89×10^{-5} (-0.0234)	0.2040 (1.1913)	0.0113 ^{**} (1.9868)	-0.3255 ^{***} (-3.0768)	1.261

Note(s): The table reports estimates from the regressions of monthly excess stock market returns against conditional variances and implied variance. Models (1) to (5) are estimates from the regressions without a dummy variable of uncertainty. Models (1)-E to (5)-E ((1)-V to (5)-V) are estimates from the regressions with a dummy variable of FEPV (FVOV). Newey and West (1987) corrected t -statistics are reported in parentheses. *, ** and *** represent significance at the 10, 5 and 1% levels, respectively

Table 4. Monthly excess stock market returns against conditional variances and implied variance with uncertainty

interaction term between D_t and the conditional variances or implied variance are negatively significant at the 1% or 5% levels. The adjusted R^2 s of the two-regime equation range from 1.261% to 12.482%, which is an improvement over those of the one-regime equation. The two-regime equation improvements in the adjusted R^2 s of FEPV, 3.855%p to 5.160%p, are always larger than those with FVOV, 0.924%p to 4.220%p.

Table 4 shows that considering uncertainty restores a positive mean–variance relationship across the four conditional variance models and model-free implied variance. Additionally, the impact of FEPV on the mean–variance relationship is larger than the impact of FVOV, and the results indicate that uncertainty has an important effect on the mean–variance relationship in stock markets. Therefore, we can confirm a varying mean–variance relationship depending on the level of uncertainty: The mean–variance relationship is significantly negative during high uncertainty periods, but a positive mean–variance relationship is observed during low uncertainty periods.

3.3 Return–innovation relation

We perform an indirect test for the mean–variance relationship suggested by French *et al.* (1987) and Banerjee *et al.* (2007). Specifically, a regression is conducted to measure the

relationship between future excess stock market returns and contemporaneous unexpected volatility innovations.

French *et al.* (1987) mention that if a larger conditional variance in the next month is predicted, the volatility innovation in the next month will decrease. Additionally, the variance for future periods will be revised upward. If there is a positive relationship between the risk premium and the predicted variance, the discount rate for future cash flows will increase. Thus, if cash flows are not affected, the current stock price, which is the discounted value of future cash flows from the firms, will decrease with a higher discount rate. Thus, there is a negative relationship between volatility innovation and future stock market returns if there is a positive relationship between conditional variance and future stock market returns.

Banerjee *et al.* (2007) develop a theory on the reactions of future returns to implied variance and implied variance shocks. If the price risk premium is positive and the implied variance positively predicts future realized variance, the level of implied variance and innovations of implied variance are positively related to future returns. For the VIX and S&P500 index excess returns, they provide empirical evidence that VIX is positively associated with 30-day and 60-day geometric returns on the S&P500 index. However, innovations in VIX are unrelated to future market returns.

Based on the above arguments for innovations on conditional variances and implied variance, we hypothesize a negative mean–innovation relationship in low uncertainty periods. Still, this relation is undermined in periods of high uncertainty. Additionally, we expect that innovations in VIX will positively impact future stock market returns during low uncertainty periods and negatively (or insignificantly) impact returns in periods of high uncertainty.

Before exploring these hypotheses, we first calculate the volatility innovation. Following French *et al.* (1987) and Yu and Yuan (2011), the volatility innovation in the rolling window model and MIDAS is calculated as the difference between the realized variance and the conditional variances:

$$Var(R_{t+1})^u = \sigma_{t+1}^2 - Var_t(R_{t+1}). \quad (13)$$

Additionally, Yu and Yuan (2011) employ the monthly volatility innovations of GARCH(1,1) and GJR-GARCH(1,1) as the difference between conditional variances for month $t+2$ based on conditional information at month $t+1$ and conditional information at month t . Therefore, following Yu and Yuan (2011), we calculate the volatility innovations of GARCH(1,1) and GJR-GARCH(1,1) as follows:

$$Var(R_{t+1})^u = Var_{t+1}(R_{t+2}) - Var_t(R_{t+2}) = E_{t+1} \left(\sum_{d=1}^{22} \sigma_{e(t+1)+d}^2 \right) - E_t \left(\sum_{d=23}^{44} \sigma_{e(t)+d}^2 \right). \quad (14)$$

Following Banerjee *et al.* (2007), we use the difference between the squared VIXs at month t and month $t-1$ as the innovations in the model-free implied variance:

$$Var(R_{t+1})^u = VIX_t^2 - VIX_{t-1}^2. \quad (15)$$

Based on the estimated innovations on the conditional variances and implied variance, the return–innovation relationship is examined with the following regression:

$$R_{t+1} = c + dVar_t(R_{t+1}) + eVar(R_{t+1})^u + \varepsilon_{t+1}, \quad (16)$$

where $Var_t(R_{t+1})$ is the conditional variance or implied variance of the stock market returns for the next month $t+1$ based on conditional information at month t , and $Var(R_{t+1})^u$ is the contemporaneous volatility innovation. To explore our hypotheses, we examine the following two-regime equation:

$$R_{t+1} = c_1 + d_1 Var_t(R_{t+1}) + e_1 Var(R_{t+1})^u + c_2 D_t + d_2 D_t Var_t(R_{t+1}) + e_2 D_t Var(R_{t+1})^u + \varepsilon_{t+1}, \quad (17)$$

where D_t is a dummy variable for the high uncertainty regime, the value of which equals 1 if month t is included in high uncertainty periods.

Table 5 reports the results of the regression with volatility innovation. For the conditional variances of four models in Panels A to D, most of the coefficient estimates (e_2) on the interaction term between the volatility innovation and D_t are positively significant at the 1% or 5% levels, except for the volatility innovations of conditional variances estimated by GARCH(1,1) with D_t of FEPU and GJR-GARCH(1,1) with D_t of FVOV. Although the coefficient estimates (e) on the volatility innovation are always negatively significant, the magnitude of coefficient estimates (e_1) on the volatility innovation during low uncertainty periods becomes bigger than e in models (1) to (4). Among models with the conditional variances, the improvements in the adjusted R^2 range from 4.783%p to 9.281%p with D_t of FEPU and from 2.610%p to 4.606%p with D_t of FVOV. As shown in Table 4, the increments of the adjusted R^2 by considering FEPU are always larger than those by considering FVOV in models with the conditional variances.

In model (5) of Panel E, the relationship between future stock market returns and the innovation on the implied variance is significantly negative, which is inconsistent with the theory of Banerjee *et al.* (2007). Considering the effect of uncertainty, the coefficient estimates (e_2) on the interaction term between volatility innovation and D_t are negatively significant at the 1% level. Additionally, the coefficient estimates (e_1) on volatility innovation during low uncertainty periods are positively significant at the 1% or 10% levels. While the coefficient estimate (d) on the implied variance is insignificant in model (5), the coefficient estimates (d_1) on the implied variance during low uncertainty periods are positively significant at the 1% level in models (5)-E and (5)-V. In contrast to the results in models with the conditional variances, the improvement in the adjusted R^2 with exploiting FVOV is larger than that with exploiting FEPU.

To conclude, uncertainty impacts the relationship between future stock market returns and the expected variance, including the conditional variances and implied variance, and the relationship between future stock market returns and contemporaneous volatility innovations. We confirm that a negative relationship between the return and innovation of the conditional variance and a positive relationship between the return and the innovation of the implied variance are significant during low uncertainty periods. Conversely, uncertainty undermines these two relations in periods of high uncertainty. Such two-regime patterns provide indirect empirical evidence of the influence of uncertainty on the link between returns and volatility.

4. Robustness checks

In this section, we check the robustness of our empirical results. In Section 4.1, we first replace the base assets to construct a mimicking factor for uncertainty. In Section 4.2, we analyze the mean–variance relation and the return–innovation relation after controlling for the effect of investor sentiment.

Table 5.
Monthly excess stock market returns against conditional variances, implied variance and volatility innovations with uncertainty

Model	c_1	$d(d_1)$	$e(e_1)$	c_2	d_2	e_2	Adj. R^2 (%)
Panel A: Rolling window model							
(1)	0.0127*** (7.3580)	-2.4713*** (-12.1310)	-4.5140*** (-5.8518)				23.919
(1)-E	0.0141*** (6.8807)	-3.3810*** (-2.8929)	-13.1511*** (-7.0153)	0.0017 (0.4118)	0.6644 (0.5879)	9.6562*** (5.5191)	33.200
(1)-V	0.0122*** (6.3176)	-2.7114*** (-5.6440)	-7.9211*** (-4.0476)	0.0036 (0.9818)	0.1817 (0.4548)	2.7468** (2.3258)	28.109
Panel B: MIDAS							
(2)	0.0137*** (8.8590)	-3.3620*** (-11.1890)	-5.7707*** (-4.3743)				25.579
(2)-E	0.0100*** (3.5257)	-4.4473** (-2.1610)	-10.8156*** (-3.4397)	0.0074 (1.4790)	1.2914 (0.6825)	6.5161*** (2.2780)	30.525
(2)-V	0.0070** (2.4858)	-2.1715* (-1.8547)	-7.5626*** (-4.9310)	0.0098** (2.5979)	-0.5778 (-0.8695)	4.5875*** (3.5795)	30.185
Panel C: GARCH(1,1)							
(3)	0.0112*** (6.1250)	-2.2474*** (-6.9994)	-4.0364*** (-6.3578)				21.463
(3)-E	0.0069* (1.8890)	-1.4596 (-0.4567)	-8.9600*** (-2.0007)	0.0076* (1.6687)	-1.1033 (-0.3623)	5.5141 (1.2932)	26.246
(3)-V	0.0046* (2.2378)	0.4845 (0.8697)	-5.5790*** (-5.9684)	0.0098** (2.3244)	-2.9811*** (-5.9331)	2.5081*** (2.8718)	25.507
Panel D: GJR-GARCH(1,1)							
(4)	0.0111*** (4.7355)	-2.4344*** (-3.5514)	-6.3264*** (-3.7760)				26.805
(4)-E	0.0072 (2.2234)	-2.5108 (-1.0646)	-16.2551*** (-3.5881)	0.0081* (1.7952)	-0.3699 (-0.1575)	10.9728** (2.4313)	33.315
(4)-V	0.0016 (0.6390)	2.4062*** (3.1317)	-5.9096*** (-4.5766)	0.0131*** (3.1319)	-5.5449*** (-6.8486)	-1.0096 (-1.1106)	29.415
Panel E: Implied variance							
(5)	0.0059** (1.9835)	-0.0136 (-0.1229)	-0.1855** (-2.5653)				0.821
(5)-E	-0.0042 (-1.3380)	0.4625*** (4.6442)	0.2939 (1.9550)	0.0142** (2.1479)	-0.5506*** (-3.4403)	-0.4644*** (-2.6341)	4.075
(5)-V	-0.0033 (-1.1283)	0.5035*** (4.3046)	0.6882 (3.1617)	0.0134** (2.0459)	-0.4561*** (-2.9663)	-1.2897*** (-4.6225)	11.665

Note(s): The table reports estimates from the regressions of monthly excess stock market returns against conditional variances, implied variance and volatility innovations. Models (1) to (5) are estimates from the regressions with a dummy variable of uncertainty. Models (1)-E to (5)-E: (1)-V to (5)-V are estimates from the regressions with a dummy variable of FFPU (FVOV). Newey and West (1987) corrected t -statistics are reported in parentheses. *, **, and *** represent significance at the 10, 5 and 1% levels, respectively

4.1 Base assets

Lamont (2001) utilizes the return on four bond portfolios, eight industry-sorted stock portfolios, and the market portfolio for the stock market over the T-bill return as the base assets' returns for seven macroeconomic variables' mimicking factors. Ang, Hodrick, Xing, and Zhang (2006) use excess returns as the returns on the base assets to create a mimicking factor for innovation in VIX. Following them, we change the base assets from the Fama–French three factors to excess stock market returns (i.e. the market risk factor) [12].

Table 6 presents the regression results with the mimicking factor for uncertainty using excess stock market returns as the base asset's returns [13]. For the regressions of the mean–variance relationship, the coefficient estimates (b_2) on the interaction term between the variances and D_t are negatively significant at the 1% level, which undermines a positive mean–variance relationship. Although the coefficient estimates (b_1) on the variances are insignificant or significant at the 10% level, their sign is always positive, as expected. Compared with models (1) to (5) in Table 4, the changes of the adjusted R^2 range from 1.013%p to 4.252%p, which are always positive. Consistent with the results in Table 4, the results in models (1) to (5) of Table 6 indicate that the deteriorated mean–variance tradeoff is induced by uncertainty. Thus, considering uncertainty improves the explanatory power for the mean–variance relationship.

In the return–innovation relationship with four conditional variances, the coefficient estimates (e_2) on the interaction term between the volatility innovations and D_t are positively significant at the 1% or 5% levels, except for GJR-GARCH(1,1), in which the coefficient estimate (e_2) is insignificant. During low uncertainty periods, the coefficient estimates (e_1) on the innovations of the conditional variances are negatively significant at the 1% level, which is consistent with the empirical evidence in French *et al.* (1987). For the innovation of the implied variance, the coefficient estimates (e_2) are negatively significant at the 1% level, and the coefficient estimate (e_1) is positively significant at the 1% level. This positive sign of e_1 is consistent with Banerjee *et al.* (2007). The improvements in the adjusted R^2 range from 2.543%p to 10.479%p, compared with the adjusted R^2 in models (1) to (5) of Table 5. The results in models (1)-I to (5)-I of Table 6 also support our hypothesis that uncertainty weakens the return–innovation relationship. Consequently, a positive mean–variance relationship is undermined when uncertainty is high.

4.2 Investor sentiment

Yu and Yuan (2011) show the impact of investor sentiment on the mean–variance tradeoff in stock markets. They find empirical evidence that the expected stock market return is positively related to the conditional variance during low sentiment periods. Still, this positive relationship is weakened during high sentiment periods. These patterns are very similar to the results of this study. Therefore, in this subsection, the analyses in Tables 4 and 5 are repeated after controlling for the effect of investor sentiment on FEPU or FVOV. To control for the effect of investor sentiment, we perform the following regression:

$$FEPU_t(\text{or } FVOV_t) = f + gSENT_{t-1} + \eta_t(\text{or } \nu_t), \quad (18)$$

where $SENT_{t-1}$ is Baker and Wurgler's (2006) investor sentiment index at month $t-1$ [14, 15], and η_t (ν_t) is the residual FEPU (FVOV) in month t . D_t^I is a dummy variable for the high uncertainty regime based on FEPU (FVOV), the value of which equals 1 if η_t (ν_t) is positive. For equations (12) and (17), we replace D_t with D_t^I to analyze the effect of residual FEPU or residual FVOV on the mean–variance relationship and the return–innovation relationship.

Table 7 reports the regression results for the two-regime equation after controlling for the effect of investor sentiment. In models (1)-E to (5)-E, the coefficient estimates (b_2) on the interaction term between the conditional variances or the implied variance and D_t^I are

Table 6.
Effect of changing base assets: Monthly excess stock market returns against conditional variances, implied variance and volatility innovations with uncertainty

Model	$a_1(c_1)$	$b_1(d_1)$	e_1	$a_2(c_2)$	$b_2(d_2)$	e_2	Adj. R^2 (%)
Panel A: Rolling window model							
(1)	0.0047 ^{***} (2.2807)	0.7103 (0.5370)	-7.9227 ^{***} (-4.0513)	0.0091 [*] (1.8862)	-2.6101 ^{**} (-2.0908)		5.011
(1)-I	0.0122 ^{***} (6.6835)	-2.7464 ^{***} (-5.5376)		0.0044 (1.0775)	0.1885 (0.4715)	4.7460 ^{**} (2.3193)	28.202
Panel B: MIDAS							
(2)	6.16×10^{-4} (0.2073)	2.1687 (1.5972)	-7.5649 ^{***} (-4.9085)	0.0134 ^{**} (2.4910)	-3.9496 ^{***} (-3.2137)		11.574
(2)-I	0.0071 [*] (2.5341)	-2.2098 [*] (-1.8503)		0.0106 ^{**} (2.4745)	-0.5689 (-0.8406)	4.5440 ^{***} (3.5333)	30.292
Panel C: GARCH(1,1)							
(3)	7.01×10^{-4} (0.2679)	2.5984 [*] (1.6937)	-5.5747 ^{***} (-5.9793)	0.0119 ^{**} (2.3336)	-4.2979 ^{***} (-3.3846)		5.791
(3)-I	0.0046 ^{**} (2.3424)	0.4081 (0.7875)		0.0107 ^{**} (2.2613)	-2.9283 ^{***} (-6.3800)	2.4849 ^{***} (2.8758)	25.453
Panel D: GJR-GARCH(1,1)							
(4)	-4.94×10^{-4} (-0.1401)	3.4187 (1.3866)	-5.8743 ^{***} (-4.6154)	0.0159 ^{***} (2.6747)	-5.8519 ^{***} (-3.0361)		6.475
(4)-I	0.0016 (0.6730)	2.2752 ^{***} (2.8449)		0.0141 ^{***} (3.0637)	-5.4546 ^{***} (-6.4976)	-1.1363 (-1.2380)	29.348
Panel E: Implied variance							
(5)	-3.06×10^{-4} (-0.0821)	0.2038 (1.1870)	0.6606 ^{***} (2.9415)	0.0126 [*] (1.9672)	-0.3308 ^{***} (-3.1085)		1.327
(5)-I	-0.0034 (-1.2084)	0.4914 ^{***} (4.1071)		0.0148 ^{**} (2.0418)	-0.4514 ^{**} (-2.9167)	-1.2630 ^{***} (-4.4360)	11.300

Note(s): The table reports estimates from the regressions of monthly excess stock market returns against conditional variances, implied variance and volatility innovations. Models (1) to (5) are estimates from the regressions with conditional variance, implied variance and a dummy variable of FEPV or FVOV. Models (1-I) to (5-I) are estimates from the regressions with conditional variance, implied variance, volatility innovations and a dummy variable of FEPV or FVOV. [Newey and West \(1987\)](#) corrected t -statistics are reported in parentheses. *, **, and *** represent significance at the 10, 5 and 1% levels, respectively

Model	a_1	b_1	a_2	b_2	Adj. R^2 (%)
Panel A: Rolling window model					
(1)-E	0.0020 (0.7564)	3.8492 ^{***} (4.5014)	0.0089 [*] (1.7045)	-5.7503 ^{***} (-7.7159)	8.640
(1)-V	-7.12×10^{-4} (-0.2854)	4.3781 ^{***} (6.3711)	0.0142 ^{***} (3.7523)	-6.4427 ^{***} (-11.3850)	10.498
Panel B: MIDAS					
(2)-E	1.59×10^{-4} (0.0555)	3.2272 ^{***} (5.9357)	0.0107 ^{**} (2.1665)	-4.9393 ^{***} (-8.3578)	12.596
(2)-V	-0.0015 (-0.5874)	3.1987 ^{***} (5.3412)	0.0146 ^{***} (3.9200)	-4.9571 ^{***} (-8.2909)	12.819
Panel C: GARCH(1,1)					
(3)-E	4.81×10^{-4} (0.1732)	3.7434 ^{***} (6.2314)	0.0091 [*] (1.8885)	-5.3781 ^{***} (-8.5842)	7.239
(3)-V	-0.0018 (-0.6836)	3.9706 ^{***} (6.0568)	0.0137 ^{***} (3.6034)	-5.7159 ^{***} (-8.8836)	8.097
Panel D: GJR-GARCH(1,1)					
(4)-E	-0.0019 (-0.6117)	5.4890 ^{***} (6.1301)	0.0137 ^{***} (2.8953)	-7.7743 ^{***} (-7.5828)	7.938
(4)-V	-0.0044 (-1.4859)	5.7892 ^{***} (5.9516)	0.0189 ^{***} (4.4732)	-8.2731 ^{***} (-8.3799)	9.255
Panel E: Implied variance					
(5)-E	-0.0042 (-1.1450)	0.4054 ^{***} (6.2509)	0.0138 ^{**} (2.0619)	-0.5294 ^{***} (-3.6461)	4.232
(5)-V	-0.0064 [*] (-1.8488)	0.4188 ^{***} (6.2855)	0.0191 ^{***} (3.4688)	-0.5658 ^{***} (-4.1600)	4.991

Note(s): The table reports estimates from the regressions of monthly excess stock market returns against conditional variances, and implied variance. Models (1)-E to (5)-E ((1)-V to (5)-V) are estimates from the regressions with a dummy variable of FEPU (FVOV) after removing the effect of investor sentiment. [Newey and West \(1987\)](#) corrected t -statistics are reported in parentheses. *, **, and *** represent significance at the 10, 5 and 1% levels, respectively

Table 7. Removing effect of investor sentiment: Monthly excess stock market returns against conditional variances and implied variance with uncertainty

negatively significant at the 1% level. Additionally, the coefficient estimates (b_1) on the conditional variances or implied variance are positively significant at the 1% level. In models (1)-V to (5)-V, the patterns of b_1 and b_2 are similar to those in models (1)-E to (5)-E. Furthermore, including D_t^i of the residual FEPU significantly improves the adjusted R^2 , with a minimum and maximum increase of 4.462%p and 5.274%p, respectively. The improvements of the adjusted R^2 by exploiting the dummy variable of the residual FVOV range from 5.221%p to 6.500%p. These results in [Table 7](#) are very similar to those of the two-regime mean–variance equations in [Table 4](#).

In [Table 8](#), we repeat the analysis for the return–innovation relationship in [Table 5](#) with the dummy variables of the residual FEPU and residual FVOV. The results in [Table 8](#) are similar to the two-regime return–innovation equations results with D_t^i in [Table 5](#). The coefficient estimates (e_2) on the interaction term between the innovation on the conditional variances and D_t^i are positively significant at the 1% or 5% levels, except for GARCH(1,1), while the coefficient estimates (e_2) in the models with the innovation on the implied variance are negatively significant at the 1% level. During low uncertainty periods, the relationship between the return and volatility innovation is restored. Additionally, the adjusted R^2 s of all models in [Table 8](#) are substantially improved by utilizing the dummy variable of uncertainty. Thus, these results confirm that including the dummy variable of uncertainty is valuable, regardless of controlling for the effect of investor sentiment on uncertainty.

Table 8.
Removing effect of investor sentiment: Monthly excess stock market returns against conditional variances, implied variance and volatility innovations with uncertainty

Model	c_1	d_1	e_1	c_2	d_2	e_2	Adj. R^2 (%)
Panel A: Rolling window model							
(1)-E	0.0143 ^{***} (4.3058)	-3.4188 [*] (-1.8759)	-13.2368 ^{***} (-3.8734)	1.90×10^{-4} (0.0412)	0.7225 (0.4162)	9.5675 ^{***} (3.2284)	31.399
(1)-V	0.0121 ^{***} (5.6033)	-3.2181 [*] (-2.2054)	-13.7670 ^{***} (-5.1744)	0.0050 (1.5078)	0.3754 (0.2703)	10.16669 ^{***} (4.7905)	34.020
Panel B: MIDAS							
(2)-E	0.0092 ^{***} (2.9226)	-3.9062 ^{**} (-2.2572)	-10.2324 ^{***} (-3.6569)	0.0069 (1.5717)	0.6855 (0.4357)	5.6301 ^{**} (2.0558)	28.987
(2)-V	0.0075 ^{**} (2.5693)	-3.9094 ^{***} (-2.8645)	-10.3914 ^{***} (-5.2312)	0.0110 ^{***} (2.7000)	0.5951 (0.4947)	5.6541 ^{**} (2.5860)	30.064
Panel C: GARCH(1,1)							
(3)-E	0.0061 ^{**} (2.2994)	-0.7111 (-0.3360)	-7.7869 ^{**} (-2.5052)	0.0072 [*] (1.8518)	-1.8344 (-0.9071)	4.2459 (1.4379)	25.026
(3)-V	0.0039 (1.3602)	-0.3096 (-0.1308)	-7.7298 ^{**} (-2.0614)	0.0117 ^{***} (3.0021)	-2.3555 (-1.0219)	4.1537 (1.1668)	26.165
Panel D: GJR-GARCH(1,1)							
(4)-E	0.0057 ^{**} (2.1069)	-1.3302 (-0.6801)	-14.6554 ^{***} (-3.3564)	0.0083 ^{**} (2.0916)	-1.5325 (-0.8016)	9.2307 ^{***} (1.9759)	31.857
(4)-V	0.0051 [*] (1.8725)	-1.6682 (-0.9629)	-16.2106 [*] (-4.3438)	0.0110 ^{***} (2.8526)	-1.3415 (-0.8714)	10.9692 [*] (2.4663)	34.568
Panel E: Implied variance							
(5)-E	-0.0045 (-1.6060)	0.5485 ^{***} (8.8157)	0.4491 ^{***} (3.3723)	0.0135 ^{**} (2.5122)	-0.6336 ^{**} (-6.0791)	-0.6226 ^{***} (-3.5389)	5.521
(5)-V	-0.0063 (-2.1060)	0.5542 ^{***} (8.1905)	0.4601 ^{***} (3.6592)	0.0186 ^{***} (3.9672)	-0.6589 ^{***} (-5.5696)	-0.6525 ^{***} (-3.6574)	6.546

Note(s): The table reports estimates from the regressions of monthly excess stock market returns against conditional variances, implied variance and volatility innovations. Models (1)-E to (5)-V are estimates from the regressions with a dummy variable of FEPV (FVOV) after removing the effect of investor sentiment. Newey and West (1987) corrected t -statistics are reported in parentheses. *, **, and *** represent significance at the 10, 5 and 1% levels, respectively

5. Conclusion

This study examines the impact of uncertainty on the mean–variance tradeoff—high uncertainty undermines a positive tradeoff—which is further confirmed by the weakness of a negative relationship between contemporaneous innovations of conditional variances with stock market returns and a positive relationship of contemporaneous innovations of the implied variance with stock market returns during periods of high uncertainty. Additionally, our findings are robust to the change in the base assets used to construct the mimicking factor for uncertainty and the elimination of the influence of investor sentiment from uncertainty. Our empirical evidence is consistent with high ambiguity aversion and risk perception for investors, high cash flow risk and unfavorable investment opportunities, and the leverage effect during periods of high uncertainty.

Our paper extends the research on the asset pricing implications of option-implied uncertainty and risk. VOV and the implied variance have different information compared with EPU and the conditional variances, respectively. Therefore, we check the influence of VOV on the risk–return relationship and the relationship of the implied variance with stock market return depending on the level of uncertainty. Additionally, we provide a novel algorithm in which the information extracted from the options market, such as uncertainty and risk, exerts influence on the asset pricing model with rational investors and compensation for bearing risk.

Our study also suggests an additional perspective on portfolio management and policymaking. It is possible to apply uncertainty in making decisions regarding asset allocation and practical risk management. In addition, one policy implication of our findings is that regulators should require financial institutions to acknowledge the effect of uncertainty on risk measurement. For example, the impact of uncertainty can be considered when estimating value-at-risk (e.g. [Xu et al., 2021](#)), and the policymakers in the stock exchange should build the standard for the margin requirements based on value-at-risk estimates considering the level of uncertainty. Furthermore, researchers should reach a consensus on the measure of uncertainty. Although EPU and VOV show similar results in this study, the mechanisms of uncertainty impacting the risk–return relationship are different. We leave the further investigation to improve the measure of uncertainty to future research.

Notes

1. Prior literature including [Baker et al. \(2016, 2020\)](#), [Gulen and Ion \(2016\)](#), [Mueller et al. \(2017\)](#), [Sharif et al. \(2020\)](#), [Jiang and Kim \(2021\)](#), [Kim \(2021\)](#) and [Yang and Yang \(2021\)](#) utilizes EPU as the measure of policy- or economic-related uncertainty.
2. [Knight \(1921\)](#) describes that risk is defined as a situation in which the investor has an unknown outcome of the investment, but the distribution of its outcome is known, and (Knightian) uncertainty is defined as a situation in which the investor has an unknown outcome of the investment and unknown distribution of the outcome. Previous literature including [Park \(2015\)](#), [Andreou et al. \(2018\)](#), [Baltussen et al. \(2018\)](#), [Kim \(2018\)](#), [Borochin and Zhao \(2019\)](#), [Dubinsky et al. \(2019\)](#), [Hollstein et al. \(2019\)](#), [Jeon et al. \(2020\)](#) and [Ruan \(2020\)](#) employs VOV as Knightian uncertainty about volatility.
3. Prior literature including [Yu and Yuan \(2011\)](#), [Kim et al. \(2014\)](#), [Seo and Kim \(2015\)](#), [Kim et al. \(2017a, b\)](#) investigates the effect of investor sentiment on asset pricing and volatility forecasting.
4. A detailed explanation for the investor channels is available in Section 2 of [Yang and Yang \(2021\)](#).
5. [Wu and Lee \(2015\)](#) find that during bear market periods, there is a negative risk–return relationship in the US stock market and argue that the leverage effect may play an important role in such periods so that the negative mean–variance relationship in bear markets may be a response to the stronger leverage effect.

6. www.policyuncertainty.com
7. https://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html
8. The correlations of the stock market return with the variances range from 0.2663 to 0.3072 during low uncertainty periods (i.e. the period with negative FEPV). During high uncertainty periods (i.e. the period with positive FEPV), the correlations of the stock market return with the variances range from -0.4074 to -0.1583 .
9. In low uncertainty periods (i.e. the period with negative FVOV), the correlations of the stock market return with the variance range from 0.0602 to 0.1958. During high uncertainty periods (i.e. the period with positive FVOV), the correlations of the stock market return with the variances range from -0.4674 to -0.1680 .
10. Our results are unaffected by another definition of D_t : if $FEPV_t$ or $FVOV_t$ is higher than the median of the monthly FEPV or FVOV over the whole sample period, then D_t equals 1, and 0 otherwise. These results are available upon request.
11. Further, we check the results with D_t depending on the level of EPU_t or VOV_t : if EPU_t or VOV_t is higher than the median of the monthly EPU or VOV over the whole sample period, then D_t equals 1, and 0 otherwise. These results are consistent with our findings and are available upon request.
12. Following [Ang et al. \(2006\)](#), we check the robustness of our results utilizing the equal-weighted and value-weighted returns of the six Fama–French 3×2 portfolios sorted on size and book-to-market as the base assets' return. These results are qualitatively similar to the results in [Tables 4 and 5](#) and available upon request.
13. When we employ the excess stock market returns as the base asset's returns, the time-series on D_t of FEPV are identical to those on D_t of FVOV. Thus, we only report the results for D_t of FEPV or FVOV.
14. The monthly investor sentiment index is obtained from the website of Jeffrey Wurgler (<http://people.stern.nyu.edu/jwurgler/>).
15. [Yu and Yuan \(2011\)](#) define the current year as a high sentiment year if the prior years' investor sentiment index is positive. Similarly, we employ the prior months' investor sentiment index to remove the effect of the investor sentiment index from the mimicking factor for uncertainty.

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